

Learning approach to optical tomography

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Received 20 February 2015; revised 24 April 2015; accepted 29 April 2015 (Doc. ID 234975); published 28 May 2015

Optical tomography has been widely investigated for biomedical imaging applications. In recent years optical tomography has been combined with digital holography and has been employed to produce high-quality images of phase objects such as cells. In this paper we describe a method for imaging 3D phase objects in a tomographic configuration implemented by training an artificial neural network to reproduce the complex amplitude of the experimentally measured scattered light. The network is designed such that the voxel values of the refractive index of the 3D object are the variables that are adapted during the training process. We demonstrate the method experimentally by forming images of the 3D refractive index distribution of HeLa cells. © 2015 Optical Society of America

OCIS codes: (180.1655) Coherence tomography; (180.3170) Interference microscopy; (180.6900) Three-dimensional microscopy; (100.3010) Image reconstruction techniques.

<http://dx.doi.org/10.1364/OPTICA.2.000517>

1. INTRODUCTION

The learning approach to imaging we describe in this paper is related to adaptive techniques in phased antenna arrays [1], iterative imaging schemes [2,3], and inverse scattering [4,5]. In the optical domain an iterative approach was demonstrated by the Sentenac group [6,7], who used the coupled dipole approximation [8] for modeling light propagation in inhomogeneous media (a very accurate method but computationally intensive) to simulate light scattering from small objects ($1\ \mu\text{m} \times 0.5\ \mu\text{m}$) in a point scanning microscope configuration. Maleki and Devaney in 1993 [9] demonstrated diffraction tomography using intensity measurements and iterative phase retrieval [10]. Very recently an iterative optimization method was demonstrated [11] for imaging 3D objects using incoherent illumination and intensity detection. There are similarities but also complementary differences between our method and [11]. Our method uses coherent light and relies on digital holography [12,13] to record the complex amplitude of the field, whereas direct intensity detection is used in [11]. Both use the beam propagation method (BPM) [14,15] to model the scattering process and the error backpropagation method [16] to train the system. At the end of the training process the network discovers a 3D index distribution that is consistent with the experimental observations. We experimentally demonstrate the technique by imaging polystyrene beads and HeLa and hTERT-RPE1 cells.

The holographic recording employed in the method presented in this paper is advantageous for imaging phase objects such as the cells in the experiments. Moreover we included in this optimization algorithm sparsity constraints that significantly improve the quality of the reconstructions. We also compared our method

with other coherent tomographic reconstruction techniques. The learning approach improved the quality of the images produced by all the direct (noniterative) tomographic reconstruction methods we tried.

2. EXPERIMENTAL SETUP

A schematic diagram of the experimental setup is shown in Fig. 1. It is a holographic tomography system [17], in which the sample is illuminated with multiple angles and the scattered light is holographically recorded. Several variations of the holographic tomography system have been demonstrated before [18–21]. The optical arrangement we used is most similar to the one described by Choi *et al.* [18]. The first beam splitter divides the laser beam in the reference and signal arms. In the signal arm a rotating mirror varies the angle of illumination of the sample using the 4F system created by L1 and OB1. The sample is imaged onto the CMOS camera using the 4F system created by OB2 and L2. The reference beam is combined with the signal beam via the beam splitter (BS2) to form a hologram. Phase stability is maintained by using a differential measurement between the phase on a portion of the field of view on the detector that does not include the cell and the cell itself. In this way the system is insensitive to drifts in the relative phase between the reference and signal beams. The NAs are 1.45 and 1.4 for the illumination and imaging portions of the system (OB1 and OB2), respectively.

The samples to be measured were prepared by placing polystyrene beads and cells between two glass cover slides. The samples were illuminated with a continuous collimated wave at 561 nm at 80 different angles. The amplitude and phase of

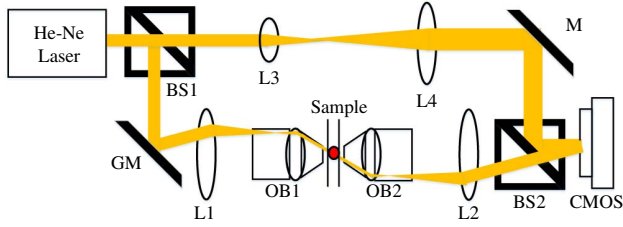


Fig. 1. Experimental setup (BS, beam splitter; GM, galva mirror; L, lens; OB, objective; M, mirror).

the light transmitted through the sample were imaged onto a 2D detector, where they were holographically recorded by introducing a reference beam. The recordings constitute the training set with which we train the computational model that simulates the experimental setup. We construct the network using the BPM. The inhomogeneous medium (beads or cells) is divided into thin slices along the propagation direction (z). The propagation through each slice is calculated as a phase modulation due to the local transverse index variation followed by propagation in a thin slice of a homogenous medium having the average value of the index of refraction of the sample.

The transverse (x - y) resolution is limited by the numerical aperture of the imaging system composed of lenses OBJ2 and L2 in Fig. 1. This limit can in principle be exceeded because the illumination is not a single plane wave. This idea was explored for conventional tomography in [22], and it could also be used in conjunction with the learning approach we describe in this paper. The longitudinal (z) resolution is limited by the numerical aperture of the illuminating beam [23].

3. METHODOLOGY

A schematic description of the BPM simulation is shown in Fig. 2. The straight lines connecting any two circles represent multiplication of the output of the unit located in the l th layer of the network at $x = n_1\delta$, $y = m_1\delta$ by the discretized Fresnel diffraction kernel $e^{j\pi((n_1^2 - n_{l+1}^2)\delta^2 + (m_1^2 - m_{l+1}^2)\delta^2)/\lambda\delta_z}$ where n_l and m_l are integers and λ is the wavelength of light. δ is the sampling

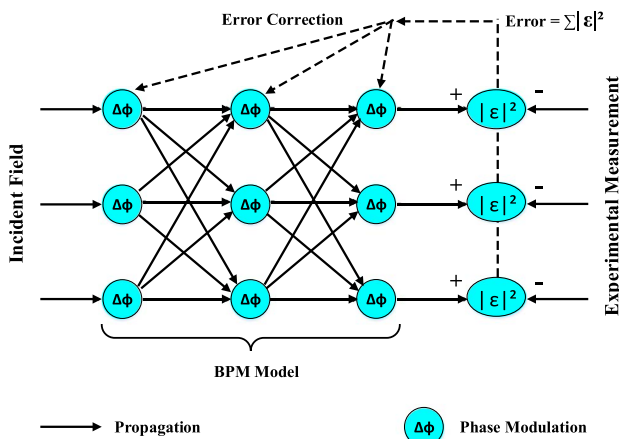


Fig. 2. Schematic diagram of object reconstruction by learning the 3D index distribution that minimizes the error ϵ , defined at the mean squared difference between the experimental measurement and the prediction of a computational model based on the BPM.

interval in the transverse coordinates (x, y), whereas δ_z is the sampling interval along the propagation direction z . The circles in the diagram of Fig. 2 perform a summation of the complex amplitude of the signals converging to each circle and also multiplication of this sum by $e^{j(2\pi\Delta n\delta_z z)/\lambda}$. $\Delta n(x, y, z)$ is the unknown 3D index perturbation of the object.

In the experiments the network has 420 layers with $\Delta n(x, y, z)$ being the adaptable variable. In contrast with a conventional neural network, the output of the layered structure in Fig. 2 is a linear function of the input complex field amplitude. However, the dependence of the output is nonlinearly related to $\Delta n(x, y, z)$. The BPM can be trained using steepest descent exactly as the backpropagation algorithm in neural networks [24–26]. Specifically, the learning algorithm carries out the following minimization:

$$\min_{\Delta\hat{n}} \left\{ \frac{1}{2K} \sum_{k=1}^K \|E_k(\Delta\hat{n}) - M_k(\Delta n)\|^2 + \tau S(\Delta\hat{n}) \right\}$$

subject to $0 \leq \Delta\hat{n}$.

In the above expression $E_k(\Delta\hat{n})$ is the current prediction of the BPM network for the output when the system is illuminated with the k th beam, and $M_k(\Delta n)$ is the actual measurement obtained by the optical system. $\Delta\hat{n}$ indicates the estimate for the index perturbation due to the object. The term $S(\Delta\hat{n})$ is a sparsity constraint [27–29] to enhance the contrast, while τ is a parameter that can be tuned to maximize image quality by systematic search. We assessed the significance of the sparsity constraint by running the learning algorithm with and without this constraint. An example of the results is shown in Fig. S4 in Supplement 1. The positivity constraint takes advantage of the assumption that the index perturbation is real and positive. The optimization is carried out iteratively by taking the derivative of the error with respect to each of the adaptable parameters following steepest descent:

$$\Delta\hat{n} \leftarrow \Delta\hat{n} - \left(\frac{\alpha}{K} \sum_{k=1}^K \epsilon_k \frac{\partial \epsilon_k}{\partial \Delta\hat{n}} + \tau \frac{\partial S(\Delta\hat{n})}{\partial \Delta\hat{n}} \right),$$

where $\epsilon_k = \|E_k(\Delta\hat{n}) - M_k(\Delta n)\|$ is the error, α is a constant, and the change in $\Delta\hat{n}$ is proportional to the error and its derivative. This is achieved efficiently via a recursive computation of the gradient, which is the backpropagation part of our learning algorithm. The data acquisition speed of this method is the same as in any other optical tomography method. It is determined by the product of the number of illumination angles and the time required to capture each hologram. The processing time to run the learning algorithm (100 iterations) after the data are recorded is more than an hour on a standard laptop computer, but it can be improved dramatically with custom signal processing circuits.

4. RESULTS

We first tested the system with polystyrene beads encapsulated between two glass slides in immersion oil. The sample was inserted in the optical system of Fig. 1, and 80 holograms were recorded by illuminating the sample at 80 distinct angles uniformly distributed in the range of -45° to $+45^\circ$. The collected data make up the training set for the 420-layer BPM network, which simulates a physical propagation distance of 30 μm and a transverse window of 37 $\mu\text{m} \times 37 \mu\text{m}$ ($\delta_x = \delta_y = 72 \text{ nm}$). The network was initialized with the standard filtered backprojection

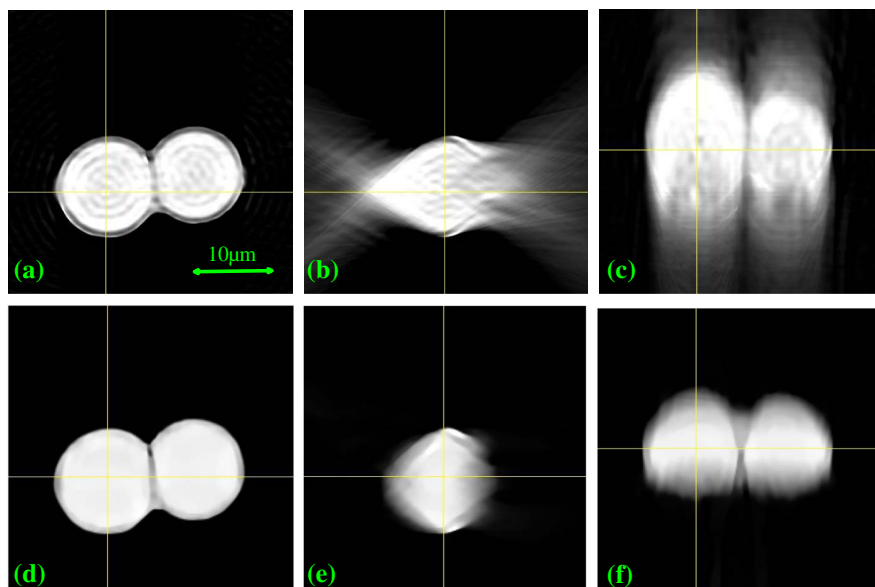


Fig. 3. Experimental reconstruction of two 10 μm beads of refractive index 1.588 at $\lambda = 561$ nm in immersion oil with $n_0 = 1.516$. (a)–(c) x–y, y–z, and x–z slices using the inverse Radon transform reconstruction. (d)–(f) Same slices for our learning-based reconstruction method. (The lines indicate the locations of the slices.)

reconstruction algorithm (Radon transform) [30], and the resulting 3D images before and after 100 iterations are shown in Fig. 3. The final image produced by the learning algorithm is an accurate reproduction of the bead shape.

The power of the learning tomography method presented in this paper is that the reconstruction of the refractive index is not based on the Born approximation. The BPM does not account for reflections, but it allows multiple forward scattering events. In the

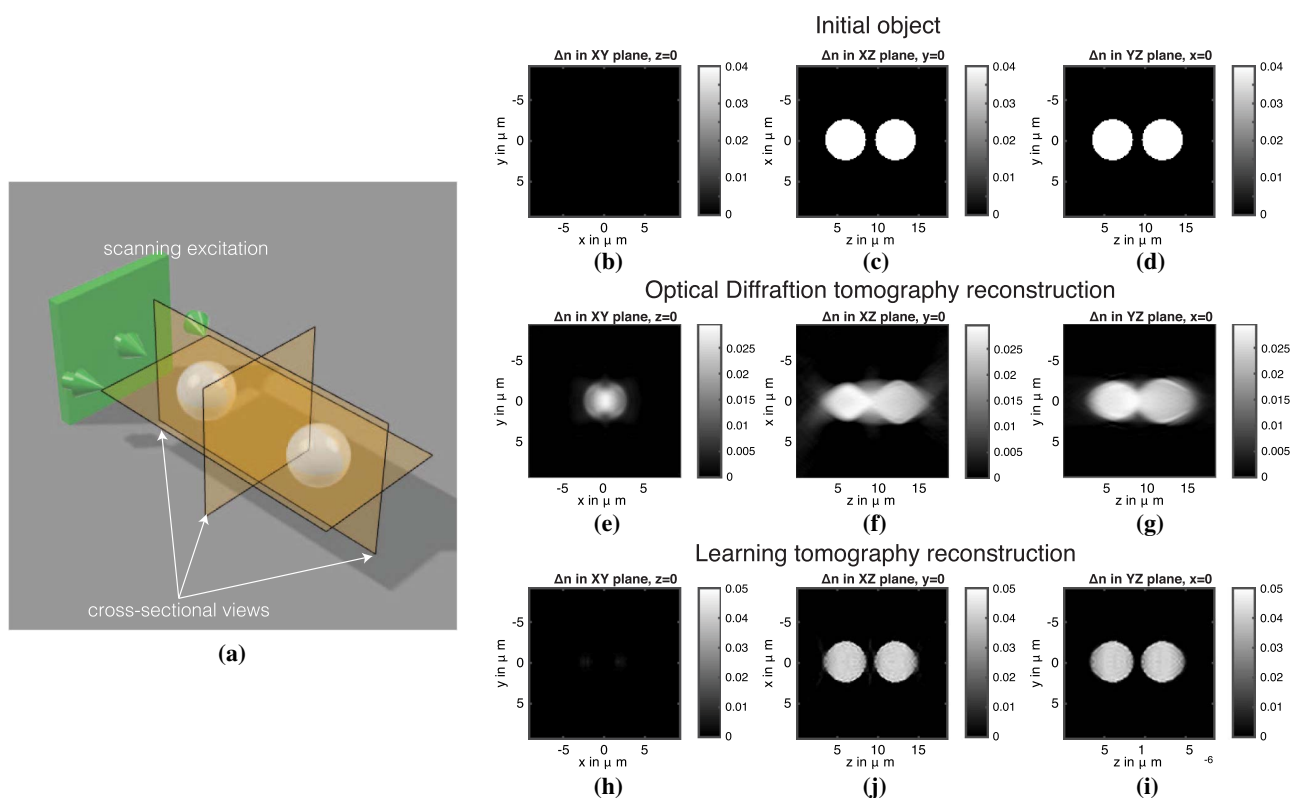


Fig. 4. Simulation geometry comprising two spherical beads with a refractive index difference of 0.04 compared to the background. (b)–(j) Cross-sectional views on x–y, x–z, and y–z planes of (b)–(d) original refractive index, (e)–(g) reconstruction with optical diffraction tomography, and (h)–(j) reconstruction with learning tomography. Because of the scattering, since the Born approximation (single scattering) is not valid, the diffraction tomography fails to reconstruct the refractive index inhomogeneity. However, the learning tomography is capable of correctly reconstructing the object.

case of multiple inhomogeneities, the Born approximation is not valid anymore and the reconstruction based on conventional tomographic techniques becomes inaccurate. In order to demonstrate this effect, we simulate a refractive index inhomogeneity ($\Delta n = 0.04$, $D = 5 \mu\text{m}$) that comprises two spherical beads on the optical axis at two different z planes. Considering the center of the computational window to be the center of the

x - y plane, the centers of the beads are placed at $x_1 = 0 \mu\text{m}$, $y_1 = 0 \mu\text{m}$, $z_1 = 6 \mu\text{m}$ and $x_2 = 0 \mu\text{m}$, $y_2 = 5 \mu\text{m}$, $z_2 = 12 \mu\text{m}$ at a distance of $6 \mu\text{m}$ away from each other. Figure 4 shows the results of the two different reconstruction schemes. Based on our previous explanation, since the Born approximation is not valid to describe the physical behavior of light propagation through this sample, the optical diffraction tomography method

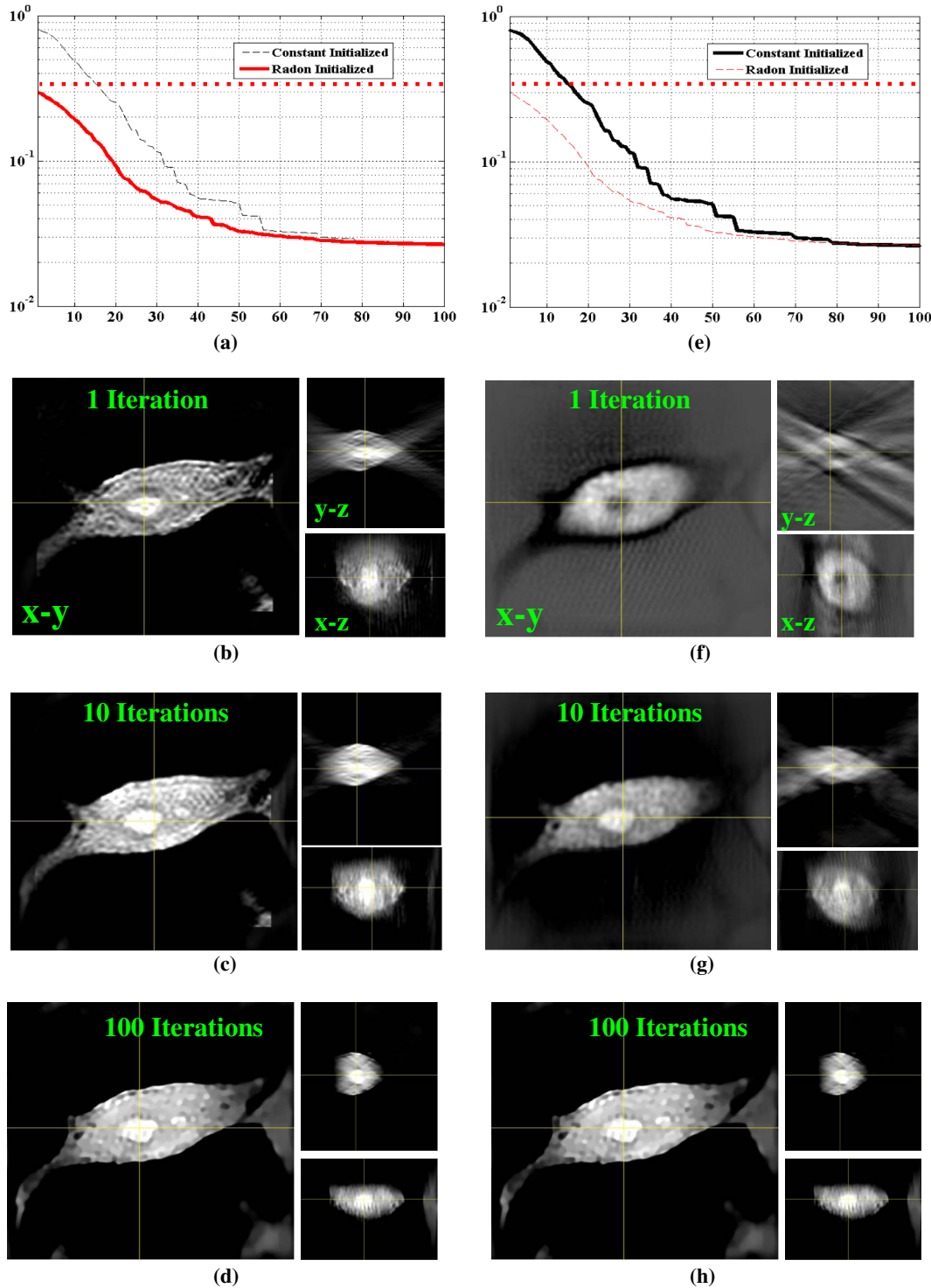


Fig. 5. Comparison of the proposed method initialized with the inverse Radon transform (left) versus initialization with a constant value ($\Delta \hat{n} = 0.007$) (right). (a) and (e) plot the error fall-off for 80 illumination angles initialized with the inverse Radon and constant values, respectively. The horizontal dotted line shows the inverse Radon performance for comparison. (b)–(d), x - y , y - z , and x - z stacks for, respectively, the first, tenth, and hundredth iterations of the proposed method initialized by inverse Radon. (d)–(f) Same figures for the proposed method initialized by constant value. (See also Media 1.)

is not capable of reconstructing the object. Contrary to that, the learning tomography method presented in this paper is capable of dealing with multiple scattering and therefore correctly reconstructs the object.

A sample of a HeLa cell was also prepared, and the same procedure was followed to obtain a 3D image. The results are shown in Fig. 5, where the error function is plotted as a function of iteration number. In this instance, the system was initialized with a constant but nonzero value ($\Delta\hat{n} = 0.007$). Also shown in Fig. 5 are the results obtained when the system was initialized with the Radon reconstruction from the same data. After 100 iterations both runs yield essentially identical results. Notice that the error in the final image (after 100 iterations) is significantly lower than the error of the Radon reconstruction. This is also evident by visual inspection of the images in Fig. 5, where the artifacts due to the missing cone [23] and diffraction [18] are removed by the learning process.

We use the result of tomographic reconstructions to initialize the learning algorithm. The results are included in Fig. 6, showing that diffraction tomography [31] and iterative Radon [18] give smaller initial error than simple Radon reconstructions but the learning algorithm in all cases reduces the error further and improves the quality of the reconstructed image. The four runs corresponding to the four different initial conditions converge to the same final reconstruction. The images corresponding to the three tomographic reconstructions used as initial conditions are presented in Supplement 1. Results from an experiment with a reduced range of illumination angles are also presented in Supplement 1.

As discussed earlier optical 3D imaging techniques rely on the assumption that the object being imaged does not significantly distort the illuminating beam. This is assumed, for example, in Radon or diffraction tomography. In other words, these 3D reconstruction methods rely on the assumption that the measured scattered light consists of photons that have only been scattered

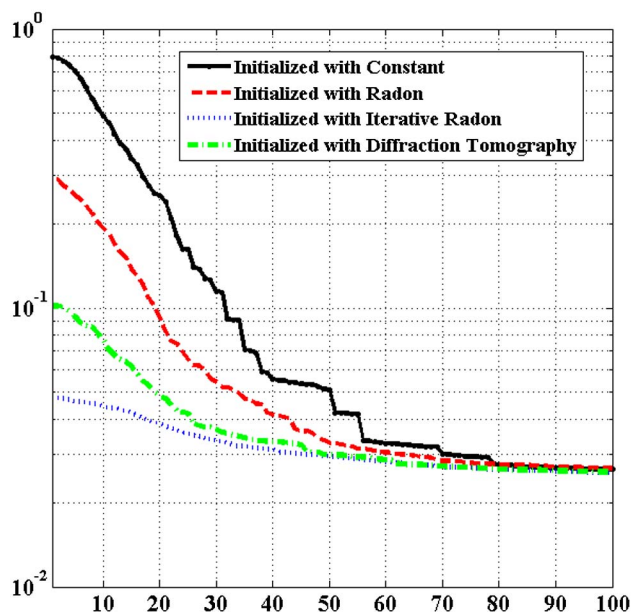


Fig. 6. Error between the experimental measurements and the predictions of the computational mode plotted as a function of the number of iterations for four different initial conditions: constant index (black), Radon tomographic reconstruction (red), diffraction tomography [31] (green), and the iterative method described in [18] (blue).

once before they reach the detector. The BPM, on the other hand, allows for multiple forward scattering events. The only simplification is that reflections are not taken into account; these could eventually be incorporated into the network equation without fundamentally altering the approach described in this paper. Since biological tissue is generally forward scattering, the BPM can be a good candidate to model propagation of thick biological samples, and this may be the most significant advantage of the learning approach. To demonstrate this point, we prepared two glass slides with a random distribution of hTERT-RPE1 cells (immortalized epithelial cells from retina) on each slide. When we attach the two slides together, we can find locations where two

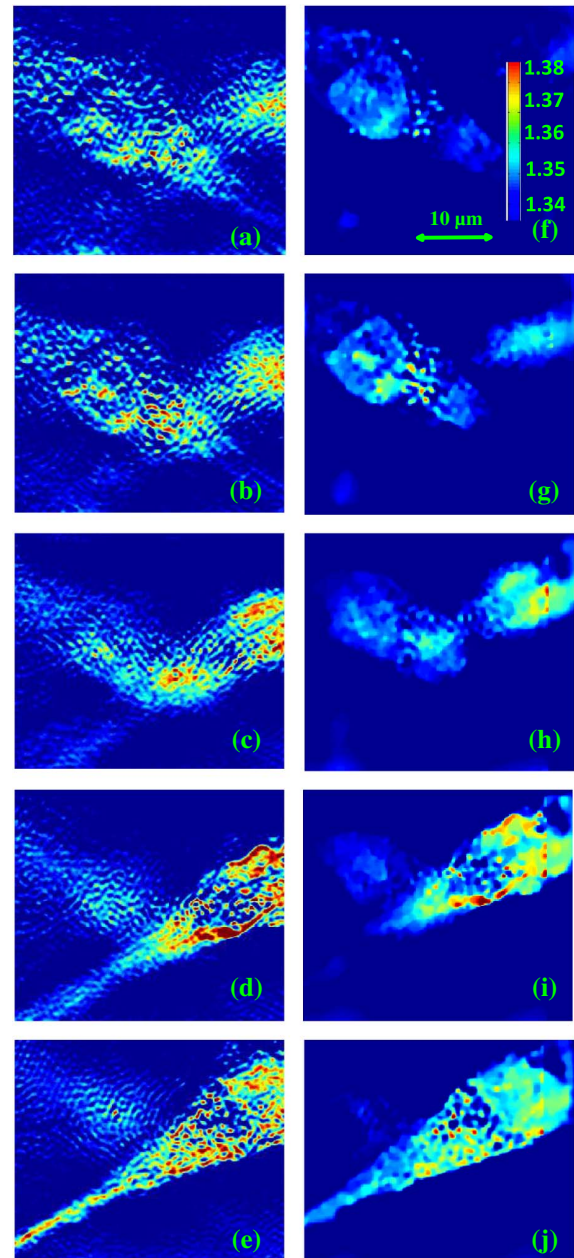


Fig. 7. Images of two hTERT-RPE1 cells. x-y slices corresponding to different depths of, respectively, +9, +6, +3, 0, and -3 μm (positive being toward the detector) from the focal plane of the lens OB2 in Fig. 1 for (a)–(e) inverse Radon-transform-based reconstruction and (f)–(j) same slices for our learning-based reconstruction method.

cells are aligned in z , one on top of the other. Figures 7(a)–7(e) show the images of such a stack of two cells produced with a direct inversion using the Radon transform. Figures 7(f)–7(j) show the same object imaged with the proposed learning algorithm. The learning method was able to distinguish the two cells where the Radon reconstruction merged the two into a single pattern due to the blurring in z , which is a consequence of the missing cone. We believe the origin of the ringing artifacts in the Radon image is due to the multiple scattering of light from one cell to another (as explained earlier).

5. DISCUSSION AND CONCLUSIONS

In conclusion, we have demonstrated a neural-network-based algorithm to solve the optical phase tomography problem and have applied it to biological (HeLa and hTERT-RPE1 cells) and synthetic (polystyrene beads) samples. The experimental measurements were performed with a conventional collimated illumination phase tomography setup, with coherent light and holograms recorded off-axis. The sample scattering potential was modeled as a neural network implementing a forward BPM. The network is organized in layers of neurons, each one of them representing an x - y plane in the BPM. The output of the network is compared to the experimental measurements, and the error is used to correct the weights (representing the refractive index contrast) in the neurons using standard error backpropagation techniques. The algorithm yields images of better quality than other tomographic reconstruction methods. In particular, the missing cone artifact is efficiently removed, as well as parasitic granular structures. We have shown that whether starting from a constant initial guess for the refractive index or with a conventional Radon tomographic image, the method essentially converges to the same result after 100 iterations. This approach opens rich perspectives for active correction of scattering in biological samples; in particular, it has the potential of increasing the resolution and the contrast in fluorescent and two-photon imaging.

European Research Council (ERC) (267439, FP7/2007-2013).

The work of U. S. Kamilov and M. Unser was supported by the European Research Council under the European Union's Seventh Framework Programme. The authors thank Phelps Edward Allen and Valérian CR Dormoy for sample preparation and Nicolino Stasio, Donald Conkey, and Ye Pu for their helpful suggestions. We also thank YongKeun (Paul) Park and Kyoohyun Kim for providing the code and assistance for optical diffraction tomography.

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See Supplement 1 for supporting content.

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