# A Learning Approach to Optical Tomography

ULUGBEK S. KAMILOV\*,1, IOANNIS N. PAPADOPOULOS\*,2, MORTEZA H. SHOREH\*,2, ALEXANDRE GOY2, CEDRIC VONESCH1, MICHAEL UNSER1, AND DEMETRI PSALTIS\*\*,2

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Optical tomography has been widely investigated for biomedical imaging applications. In recent years optical tomography has been combined with digital holography and has been employed to produce high quality images of phase objects such as cells. In this paper we describe a method for imaging 3D phase objects in a tomographic configuration implemented by training an artificial neural network to reproduce the complex amplitude of the experimentally measured scattered light. The network is designed such that the voxel values of the refractive index of the 3D object are the variables that are adapted during the training process. We demonstrate the method experimentally by forming images of the 3D refractive index distribution of Hela cells. © 2014 Optical Society of America

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# 1. INTRODUCTION

The learning approach to imaging we describe in this paper is related to adaptive techniques in phased antenna arrays [1], iterative imaging schemes [2, 3], and inverse scattering [4, 5]. In the optical domain an iterative approach was demonstrated by the Sentenac group [6, 7] who used the coupled dipole approximation [8] for modeling light propagation in inhomogeneous media (a very accurate method but computationally intensive) to simulate light scattering from small objects  $(1\mu m \times 0.5\mu m)$ in a point scanning microscope configuration. Maleki and Devaney in 1993 [9] demonstrated diffraction tomography using intensity measurements and iterative phase retrieval [10]. Very recently an iterative optimization method was demonstrated [11] for imaging 3D objects using incoherent illumination and intensity detection. There are similarities but also complementary differences between our method and [11]. Our method uses coherent light and relies on digital holography [12, 13] to record the complex amplitude of the field whereas direct intensity detection is used in [11]. Both use the Beam Propagation Method (BPM) [14, 15] to model the scattering process and the error back propagation method [16] to train the system. At the end of the

training process the network discovers a 3D index distribution that is consistent with the experimental observations. We experimentally demonstrate the technique by imaging polystyrene beads and HeLa and hTERT-RPE1 cells.

The holographic recording employed in the method presented in this paper are advantageous for imaging phase objects such as the cells in the experiments. Moreover we included in this optimization algorithm sparsity constraints which improve significantly the quality of the reconstructions. We also compared our method to other coherent tomographic reconstruction techniques. The learning approach improved the quality of the images produced by all the direct (non-iterative) tomographic reconstruction methods we tried.

# 2. EXPERIMENTAL SETUP

A schematic diagram of the experimental setup is shown in Figure 1. It is a holographic tomography system [17], in which the sample is illuminated with multiple angles and the scattered light is holographically recorded. Several variation of the holographic tomography system have been demonstrated before [18–21]. The optical arrangement we used is most similar to the

<sup>\*</sup>These authors contributed equally to the paper

<sup>&</sup>lt;sup>1</sup>Biomedical Imaging Group, École polytechnique fédérale de Lausanne, Switzerland

<sup>&</sup>lt;sup>2</sup>Optics Laboratory, École polytechnique fédérale de Lausanne, Switzerland

<sup>\*\*</sup> Corresponding author: demetri.psaltis@epfl.ch

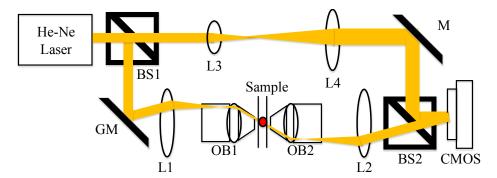


Fig. 1. Experimental setup (BS: Beam Splitter, GM: Galva Mirror, L: Lens, OB: Objective, M: Mirror)

one described by Choi *et al.* [18]. The first beam splitter divides the laser beam in the reference and signal arms. In the signal arm a rotating mirror varies the angle of illumination of the sample using the 4F system created by L1 and OB1. The sample is imaged onto the CMOS camera using the 4F system created by OB2 and L2. The reference beam is combined with the signal beam via the beamsplitter (BS2) to form a hologram. Phase stability is maintained by using a differential measurement between the phase on a portion of the field of view on the detector that does not include the cell and the cell itself. In this way the system is insensitive to drifts in the relative phase between the reference and signal beams. The NA's are 1.45 and 1.4 for the illumination and imaging portions of the system (OB1 and OB2), respectively.

The samples to be measured were prepared by placing polystyrene beads and cells between two glass cover slides. The samples were illuminated with a continuous collimated wave at 561nm at 80 different angles. The amplitude and phase of the light transmitted through the sample was imaged onto a 2D detector where it was holographically recorded by introducing a reference beam. These recordings constitute the training set with which we train the computational model that simulates the experimental setup. We construct the network using the BPM. The inhomogeneous medium (beads or cells) is divided into thin slices along the propagation direction (z). The propagation through each slice is calculated as a phase modulation due to the local transverse index variation followed by propagation in a thin slice of a homogenous medium having the average value of the index of refraction of the sample.

The transverse (x-y) resolution is limited by the numerical aperture of the imaging system comprised of lenses OBJ2 and L2 in Figure 1. This limit can in principle be exceeded because the illumination is not a single plane wave. This idea was explored for conventional tomography in [22] and it could also be used in conjunction with the learning approach we describe in this paper. The longitudinal (z) resolution is limited by the numerical aperture of the illuminating beam [23].

### 3. METHODOLOGY

A schematic description of the BPM simulation is shown in Figure 2. The straight lines connecting any two circles represent multiplication of the output of the unit located in the l-th layer of the network at  $x=n_1\delta$ ,  $y=m_1\delta$  by the discretized Fresnel diffraction kernel  $e^{j\pi[(n_l^2-n_{l+1}^2)\delta^2+(m_l^2-m_{l+1}^2)\delta^2]/\lambda\delta_z}$  where  $n_l$  and  $m_l$  are integers and  $\lambda$  is the wavelength of light.  $\delta$  is the sampling interval in the transverse coordinates (x,y) whereas  $\delta_z$  is the sampling interval along the propagation direction z. The circles in the diagram of Figure 2 perform a summation of the complex

amplitude of the signals converging to each circle and also multiplication of this sum by  $e^{j(2\pi\Delta n\delta_z z)/\lambda}$ .  $\Delta n(x,y,z)$  is the unknown 3D index perturbation of the object.

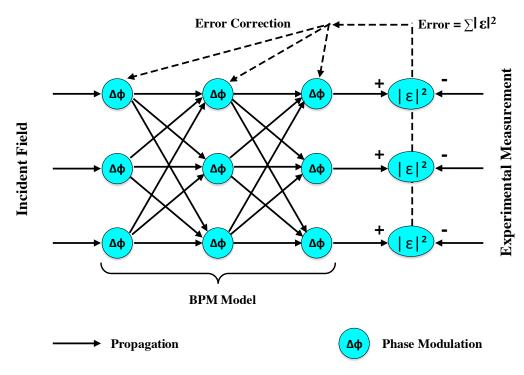
In the experiments the network has 420 layers with  $\Delta n(x,y,z)$  being the adaptable variable. In contrast with a conventional neural network, the output of the layered structure in Figure 2 is a linear function of the input complex field amplitude. However, the dependence of the output is nonlinearly related to  $\Delta n(x,y,z)$ . The BPM can be trained using steepest descent exactly as the back propagation algorithm in neural networks [24–26]. Specifically, the learning algorithm carries out the following minimization:

$$\min_{\Delta \hat{n}} \left\{ \frac{1}{2K} \sum_{k=1}^{K} \|E_k(\Delta \hat{n}) - M_k(\Delta n)\|^2 + \tau S(\Delta \hat{n}) \right\}$$
subject to  $0 \le \Delta \hat{n}$ 

In the above expression  $E_k(\Delta \hat{n})$  is the current prediction of the BPM network for the output when the system is illuminated with the k-th beam and  $M_k(\Delta n)$  is the actual measurement obtained by the optical system.  $\Delta \hat{n}$  indicates the estimate for the index perturbation due to the object. The term  $S(\Delta \hat{n})$  is a sparsity constraint [27–29] to enhance the contrast while  $\tau$  is a parameter that can be tuned to maximize image quality by systematic search. We assessed the significance of the sparsity constraint by running the learning algorithm with and without this constraint. An example of the results is shown in Figure S4 in the supplementary material section. The positivity constraint takes advantage of the assumption that the index perturbation is real and positive. The optimization is carried out iteratively by taking the derivative of the error with respect to each of the adaptable parameters following steepest descent

$$\Delta \hat{n} \leftarrow \Delta \hat{n} - \big(\frac{\alpha}{K} \sum_{k=1}^{K} \epsilon_k \frac{\partial \epsilon_k}{\partial \Delta \hat{n}} + \tau \frac{\partial S(\Delta \hat{n})}{\partial \Delta \hat{n}}\big)$$

where  $\epsilon_k = \|E_k(\Delta \hat{n}) - M_k(\Delta n)\|$  is the error,  $\alpha$  is a constant and the change in  $\Delta \hat{n}$  is proportional to the error and its derivative. This is achieved efficiently via a recursive computation of the gradient, which is the back propagation part of our learning algorithm. The data acquisition speed of this method is the same as any other optical tomography method. It is determined by the product of the number of illumination angles and the time required to capture each hologram. The processing time to run the learning algorithm (100 iterations) after the data is recorded takes more than an hour on a standard laptop computer but it can be improved dramatically with custom signal processing circuits.

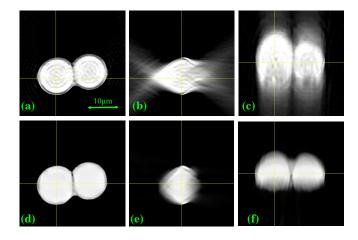


**Fig. 2.** Schematic diagram of object reconstruction by learning the 3D index distribution that minimizes the error  $\epsilon$ , defined at the mean squared difference between the experimental measurement and the prediction of a computational model based on the beam propagation method (BPM).

#### 4. RESULTS

We first tested the system with polystyrene beads encapsulated between two glass slides in immersion oil. The sample was inserted in the optical system of Figure 1 and 80 holograms were recorded by illuminating the sample at 80 distinct angles uniformly distributed in the range -45 degrees to +45 degrees. The collected data is the training set for the 420-layer BPM network which simulates a physical propagation distance of  $30\mu m$  and transverse window  $37\mu m \times 37\mu m$  ( $\delta_x = \delta_y = 72nm$ ). The network was initialized with the standard filtered back projection reconstruction algorithm (Radon transform) [30] and the resulting 3D images before and after 100 iterations are shown in Figure 3. The final image produced by the learning algorithm is an accurate reproduction of the bead shape.

The power of the learning tomography method presented in this paper is that the reconstruction of the refractive index is not based on the Born approximation. The beam propagation method does not account for reflections but it allows multiple forward scattering events. In case of multiple inhomogeneities, the Born approximation is not valid anymore and the reconstruction based on conventional tomographic techniques become inaccurate. In order to demonstrate this effect, we simulate a refractive index inhomogeneity ( $\Delta n = 0.04, D = 5\mu m$ ) that comprises of two spherical beads on the optical axis at two different z-planes. Considering the center of the computational window to be the center of the x-y plane, the center of the beads are placed at,  $x_1 = 0 \mu m$ ,  $y_1 = 0 \mu m$ ,  $z_1 = 6 \mu m$  and  $x_2 = 0 \mu m$ ,  $y_2 = 5 \mu m$ ,  $z_2 = 12 \mu m$  at a distance of  $6\mu m$  away from each other. Figure 4 shows the results of the two different reconstruction schemes. Based on our previous explanation, since the Born approximation is not valid to describe the physical behaviour



**Fig. 3.** Experimental reconstruction of two  $10\mu m$  beads of refractive index 1.588 at  $\lambda = 561nm$  in immersion oil with  $n_0 = 1.516$ . (a)-(c) x-y, y-z and x-z slices using the inverse Radon transform reconstruction, (d)-(f) the same slices for our learning based reconstruction method (The lines indicate the location of the slices).

of light propagation through this sample, the optical diffraction tomography method is not capable of reconstructing the object. Contrary to that, the Learning Tomography method presented in this paper is capable of dealing with multiple scattering and therefore correctly reconstructs the object.

A sample of a HeLa cell was also prepared and the same procedure was followed to obtain a 3D image. The results are shown in Figure 5 where the error function is plotted as a function of

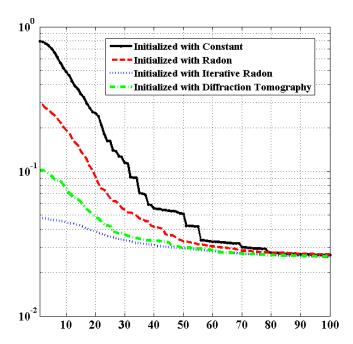
iteration number. In this instance, the system was initialized with a constant but nonzero value ( $\Delta \hat{n} = 0.007$ ). Also shown in Figure 5 are the results obtained when the system was initialized with the Radon reconstruction from the same data. After 100 iterations both runs yield essentially identical results. Notice that the error in the final image (after 100 iterations) is significantly lower than to the error of the Radon reconstruction. This is also evident by visual inspection of the images in Figure 5 where the artifacts due to the missing cone [31] and diffraction [18] are removed by the learning process.

We use the result of tomographic reconstructions to initialize the learning algorithm. The results are included in Figure 6 showing that diffraction tomography [32] and iterative Radon [18] give smaller initial error than simple Radon reconstructions but the learning algorithm in all cases reduces the error further and improves the quality of the reconstructed image. The four runs corresponding to the four different initial conditions converge to the same final reconstruction. The images corresponding to the three tomographic reconstructions used as initial conditions are presented in the supplementary material. Results from an experiment with a reduced range of illumination angles are also presented in the supplementary materials section.

As discussed earlier optical 3D imaging techniques rely on the assumption that the object being imaged does not significantly distort the illuminating beam. This is assumed for example in Radon or diffraction tomography. In other words, these 3D reconstruction methods rely on the assumption that the measured scattered light consists of photons that have only been scattered once before they reach the detector. The BPM, on the other hand, allows for multiple forward scattering events. The only simplification is that reflections are not taken into account; these could eventually be incorporated in the network equation without fundamentally altering the approach described in this paper. Since biological tissue is generally forward scattering, BPM can be a good candidate to model propagation of thick biological samples and this may be the most significant advantage of the learning approach. To demonstrate this point, we prepared two glass slides with a random distribution of hTERT-RPE1 cells (immortalized epithelial cells from retina) on each slide. When we attach the two slides together, we can find locations where two cells are aligned in z, one on top of the other. Figure 7 (a)-(e) shows the image of such a stack of two cells produced with a direct inversion using the Radon transform. Figure 7 (f)-(j) shows the same object imaged with the proposed learning algorithm. The learning method was able to distinguish the two cells where the Radon reconstruction merged the two into a single pattern due to the blurring in z which is a consequence of the missing cone. We believe the origin of the ringing artifacts in the Radon image is due to the multiple scattering of light from one cell to another (as explained earlier).

#### 5. DISCUSSIONS AND CONCLUSIONS

In conclusion, we have demonstrated a neural-network based algorithm to solve the optical phase tomography problem and have applied it to biological (HeLa and hTERT-RPE1 cells) and synthetic (polystyrene beads) samples. The experimental measurements were performed with a conventional collimated illumination phase tomography setup, with coherent light and holograms were recorded off-axis. The sample scattering potential was modeled as a neural network implementing a forward beam propagation method. The network is organised in layers



**Fig. 6.** The error between the experimental measurements and the predictions of the computational mode plotted as a function of the number of iterations for four different initial conditions: Constant index (black), Radon tomographic reconstruction (red), Diffraction tomography [32] (green) and the iterative method described [18] (blue) .

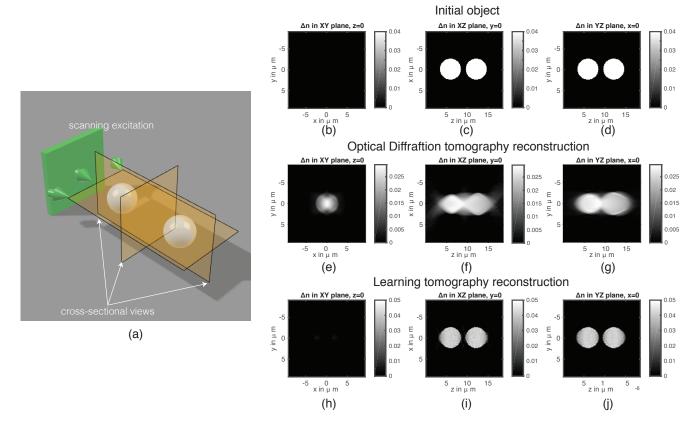
of neurons, each one of them representing an x-y plane in the BPM. The output of the network is compared to the experimental measurements and the error is used to correct the weights (representing the refractive index contrast) in the neurons using standard error back propagation techniques. The algorithm yields images of better quality than other tomographic reconstruction methods. In particular, the missing cone artefact is efficiently removed, as well as parasitic granular structures. We have shown that whether starting from a constant initial guess for the refractive index or with a conventional Radon tomographic image, the method essentially converges to the same result after 100 iterations. This approach opens rich perspectives for active correction of scattering in biological sample; in particular, it has the potential of increasing the resolution and the contrast in fluorescent and two-photon imaging.

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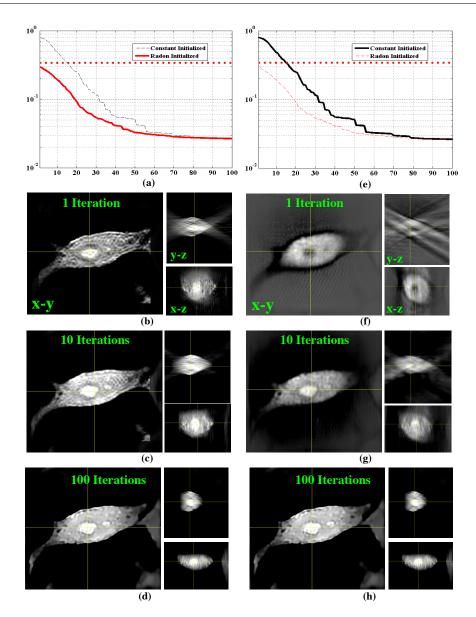


**Fig. 4.** Simulation geometry comprises of two spherical beads with a refractive index difference of 0.04 compared to the background. (b)-(j). Cross-sectional views on x-y, x-z and y-z planes of the original refractive index (b)-(d), reconstruction with Optical Diffraction Tomography (e)-(g) and Learning Tomography (h)-(j). Because of the scattering, since the Born approximation (single scattering) is not valid, the Diffraction Tomography fails to reconstruct the refractive index inhomogeneity. However, the Learning Tomography is capable of correctly reconstructing the object.

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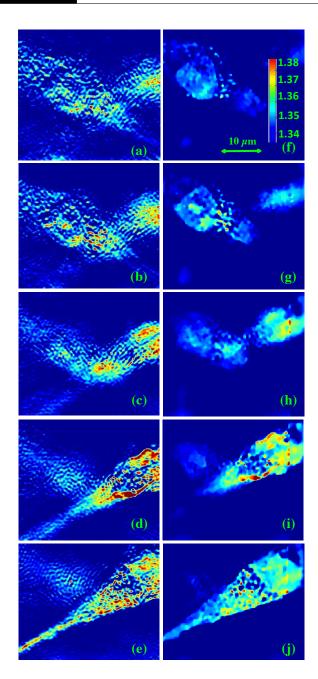
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**Fig. 5.** Comparison of the proposed method initialized with the inverse Radon transform (left) versus initialization with a constant value ( $\Delta \hat{n} = 0.007$ ) (right). Figures (a) and (e) plot the error fall-off for 80 illumination angles initialized with the inverse Radon and constant value, respectively. The horizontal doted line shows the inverse Radon performance for comparison. (b)-(d), x-y, y-z and x-z stacks for respectively the first, tenth and hundredth iteration of the proposed method initialized by inverse Radon. (d)-(f), the same figures for the proposed method initialized by constant value.

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**Fig. 7.** Images of two hTERT-RPE1 cells. x-y slices corresponding to different depths of respectively +9, +6, +3, 0 and -3 microns (positive being toward the detector) from the focal plane of the lens OB2 in Figure 1 for: (a)-(e) the inverse Radon transform based reconstruction and (f)-(j) the same slices for our learning based reconstruction method.

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